

TY Hons Maths – Homework No.6

Name of Student: _____ For _____

1. Factorise the following:

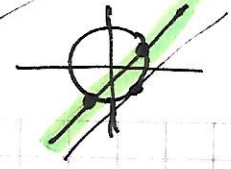
- (i) $25x^2 - 16y^2$ (ii) $a^3 - a^2b - ab^2 + b^3$ (iii) $x^4 - x$ (iv) $3x^2 - 16x + 5$

<p>(i) $25x^2 - 16y^2$ $= (5x)^2 - (4y)^2$ $= (5x + 4y)(5x - 4y)$</p>	<p>(ii) $a^3 - a^2b - ab^2 + b^3$ $a^2(a-b) - b^2(a-b)$ $(a^2 - b^2)(a-b)$ $(a-b)(a+b)(a-b)$</p>
<p>(iii) $x^4 - x$ $= x(x^3 - 1)$ $= x(x-1)(x^2 + x + 1)$ $a^3 - b^3 = (a-b)(a^2 + ab + b^2)$</p>	<p>(iv) $3x^2 - 16x + 5$ $\left \begin{array}{l} 5 \\ 15 \end{array} \right.$ $(3x-1)(x-5)$ $\begin{array}{c} -x \\ -15x \end{array}$</p>

2. Solve the following systems of simultaneous equations:

$$\begin{cases} x^2 + y^2 = 13 \\ x - y = 1 \end{cases}$$

✓



$$y = x - 1$$

$$x^2 + y^2 = 13$$

$$x^2 + (x-1)^2 = 13$$

$$x^2 + x^2 - 2x + 1 = 13$$

$$2x^2 - 2x - 12 = 0$$

$$x^2 - x - 6 = 0$$

$$(x-3)(x+2) = 0$$

$$(x-3)(x+2) = 0$$

$$x-3 = 0$$

$$x = 3$$

$$y = x - 1$$

$$y = 3 - 1$$

$$y = 2$$

$$(3, 2)$$

$$x+2 = 0$$

$$x = -2$$

$$y = x - 1$$

$$y = -2 - 1$$

$$y = -3$$

$$(-2, -3)$$

3.

The number of penguins, P , after t years in a new colony can be found using the following formula.

$$P = a \times 2^t$$

- (i) If there are 24 penguins after two years, find the value of a .
- (ii) How many years will it take for the number of penguins to first exceed 1500?

$$(i) P = 24, t = 2$$

$$P = a \times 2^t$$

$$24 = a \times 2^2$$

$$24 = a \times 4$$

$$a = \frac{24}{4} = 6$$

$$(ii) P = 6 \times 2^t$$

$$1500 = 6 \times 2^t$$

$$2^t = \frac{1500}{6} = 250$$

$$2^t = 250$$

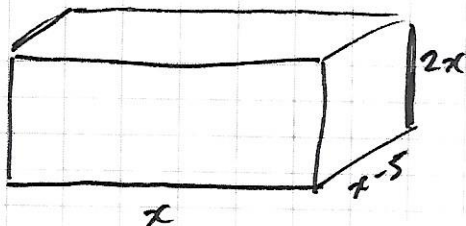
$$2^8 > 250$$

128

$$2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 256$$

4. The width of an open rectangular box is 5cm shorter than its length. The height of the box is twice the length. By letting x equal the length of the box, answer the following:

- (i) Write down the volume of the box, $V(x)$, in terms of x .
- (ii) What is the volume when $x = 7\text{cm}$.
- (iii) Why can't the box have a length less than 5cm?



$$\begin{aligned} (i) V(x) &= x(x-5)(2x) \checkmark \\ &= 2x^2(x-5) \\ &= 2x^3 - 10x^2 \end{aligned}$$

$$\begin{aligned} (ii) V(7) &= 2(7)^3 - 10(7)^2 = \\ &= 7(7-5)(14) \\ &= 196 \text{ cm}^3 \end{aligned}$$

$$(iii) x < 5$$

$$x - 5 > 0$$

$$x > 5$$