## TY Hons Maths - Homework No. 6

Name of Student: $\qquad$ For

1. Factorise the following:
(i) $25 x^{2}-16 y^{2}$
(ii) $a^{3}-a^{2} b-a b^{2}+b^{3}$
(iii) $x^{4}-x$
(iv) $3 x^{2}-16 x+5$

2. Solve the following systems of simultaneous equations: $\left\{\begin{array}{l}x^{2}+y^{2}=13 \\ x-y=1\end{array}\right.$
3. 

The number of penguins, $P$, after $t$ years in a new colony can be found using the following formula.

$$
P=a \times 2^{t}
$$

(i) If there are 24 penguins after two years, find the value of $a$.
(ii) How many years will it take for the number of penguins to first exceed 1500 ?

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4. The width of an open rectangular box is 5 cm shorter than its length. The height of the box is twice the length. By letting $x$ equal the length of the box, answer the following:
(i) Write down the volume of the box, $V(x)$, in terms of $x$.
(ii) What is the volume when $x=7 \mathrm{~cm}$.
(iii) Why can't the box have a length less than 5 cm ?
